

Discussion of “Optimal Monetary Policy with  $r^* < 0$   
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## Setting: NK model with $r^* < 0$

$$\text{NKPC:} \quad \pi_t = \beta E_t \pi_{t+1} + \kappa y_t$$

$$\text{IS:} \quad y_t = E_t y_{t+1} - \frac{1}{\sigma} [i_t - E_t \pi_{t+1} - r_t^n]$$

$$\text{ZLB:} \quad i_t \geq 0$$

$$\text{Natural rate:} \quad r_t^n = r^* + z_t, \quad r^* < 0, \quad z_t \text{ stationary.}$$

$$\text{Welfare:} \quad \frac{1}{2} E_0 \sum_{t=0}^{\infty} \beta^t (\pi_t^2 + \vartheta y_t^2).$$

Flex-price steady state efficient.

# Optimal policy and implementation

## Optimal policy: (1) the steady state

- ▶ What is socially costly?
  - ▶ Working too much ( $mrs > mrt$ ).
  - ▶ Price dispersion.
- ▶ Price dispersion linked to level of inflation (no indexation).
- ▶ NKPC: one-to-one mapping between inflation and output.
- ▶ Optimal policy: keep  $\pi$  as close to 0 as possible.
- ▶ Fisher equation  $\pi_{ss} = i_{ss} - r_{ss}^* = i_{ss} + x$ .
- ▶ To minimize social costs, set  $i_{ss} = 0$ .

## Results for the steady state c'td

- ▶  $\pi_{ss} = -r^* > 0$ .
- ▶  $y_{ss} = \frac{1-\beta}{\kappa} \pi_{ss} > 0$  (if NKPC not vertical in LR).

## Optimal policy: (2) the transition

- ▶ Realize in  $t = 0$  that  $r^* < 0$
- ▶ Reoptimize (not bound by past commitment)

## Optimal policy: (2) the transition cont'd

- ▶ iterate NKPC forward:  $\pi_t = \kappa [y_t + \beta E_t y_{t+1} + \dots + \beta^{T-1} E_t y_{t+T-1}] + \beta^T E_t \pi_{t+T}$
- ▶ Inevitable to let  $\pi$  rise above 0 eventually..
- ▶ But push inflation out to the future as much as is possible.
- ▶ Short-term recession (or smaller boom)

## An example

- ▶ Central bank controls economic activity (IS).
- ▶ Suppose it sets interest rate such that

$$y_t = y_{ss} + \alpha^t(y_0 - y_{ss}),$$

$$y_0 < y_{ss}, \alpha \in (0, 1).$$

- ▶ Then (NKPC)

$$\pi_t = \pi_{ss} + \frac{\kappa}{1 - \beta\alpha}(y_t - y_{ss}).$$

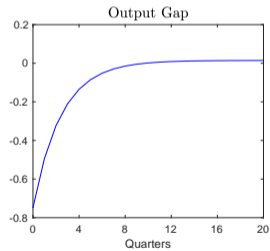
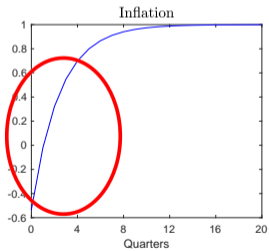
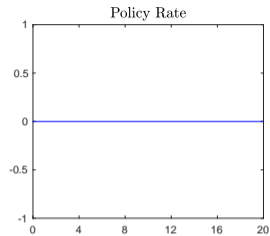
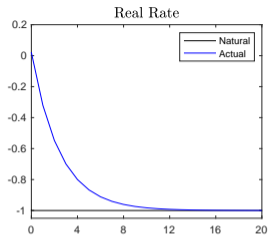


## An example cont'd

- ▶ And

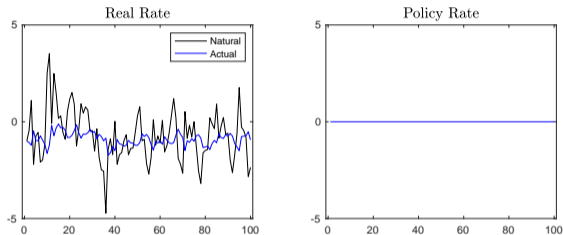
$$i_t = (y_t - y_{ss}) \left[ \underbrace{\frac{\kappa\alpha}{1 - \beta\alpha}}_{\text{expected inflation}} - \underbrace{(1 - \alpha)}_{\text{output growth}} \sigma \right]$$

- ▶ Keep inflation low  $\Rightarrow y_t < y_{ss}$ .
- ▶ Term in square brackets strictly increasing in  $\alpha$  (persistence).
- ▶ Since  $i_t \stackrel{!}{\geq} 0$  (ZLB), if  $y_t < y_{ss}$  upper bound on persistence
- ▶ Note that for  $\alpha$  such that  $[...] = 0$  (expected inflation and output growth just balance), can choose arbitrary  $y_0$  – and have  $i_t = 0$  always.



**Discretionary policy would have short-term inflation bias.**

## Optimal policy: (3) with business cycle shocks



► **Question 1: What is wrong with the buffer logic?**

## Optimal policy: (4) implementation

- ▶ Constant interest rates  $\Rightarrow$  indeterminacy.
- ▶ Which simple rule could uniquely implement the Ramsey-optimal outcome?
- ▶ Set

$$i_t = \phi_\pi |\pi_t - \pi_t^{opt}| + \phi_y |y_t - y_t^{opt}|$$

- ▶ Paper shows sufficient conditions for local determinacy.
- ▶ These are satisfied if  $\phi_y \gg 0$ .

## Optimal policy: (4) implementation cont'd

$$i_t = \phi_\pi |\pi_t - \pi_t^{opt}| + \phi_y |y_t - y_t^{opt}|, \phi_y \gg 0$$

- ▶ **Question 2: What is the economic rationale?**
- ▶ Positive non-fundamental shock: suppose expect non-fundamental output boom. Would come with higher inflation (NKPC), and higher inflation expectations (thus, lower real rate). If CB raises nominal rate enough, makes sure to invalidate expectations of a boom.
- ▶ Negative non-fundamental shock: CB *raises* rate if recessionary beliefs. That is, raises real rates ever further. Renders any (finite) recessionary expectation irrational, saying “whatever bad you believe, I will make sure that things will turn out even worse.” Boundedness rules out ever worse outcomes; this renders equilibrium determinate.

## Optimal policy: (4) implementation cont'd

$$i_t = \phi_\pi |\pi_t - \pi_t^{opt}| + \phi_y |y_t - y_t^{opt}|, \phi_y \gg 0$$

- ▶ Logic not constrained to the case  $r_t^n < 0$  or to indexing to the optimal  $\pi_t, y_t$ .
- ▶ That is, determinacy would hold with and without ZLB.
- ▶ **Question 3: Link to NK model with symmetric response**
- ▶ In the NK model, with symmetric policy, we typically focus on  $\phi_y > 0$ .
- ▶ Note that  $\phi_y < 0$  also prevents AR(1) sunspots (same logic as above).

## Optimal policy: (4) implementation cont'd

- ▶ **Question 4: Nominal indeterminacy and positive output deviation.**
- ▶ NK model with symmetric rule:  $\phi_y \rightarrow \infty$  rules out real indeterminacy, but *nominal* indeterminacy?
- ▶ Why does  $\phi_y \gg 0$  rule out real *and* nominal indeterminacy here?
- ▶ Explanation for the output boom branch?

super-interesting paper