

Housing price indices for small areas

NBP International Workshop

Recent trends in Real Estate Market and its Analysis

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Zalesie Górne,
December, 5, 2019

Outline

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- Increased information needs for policy making.

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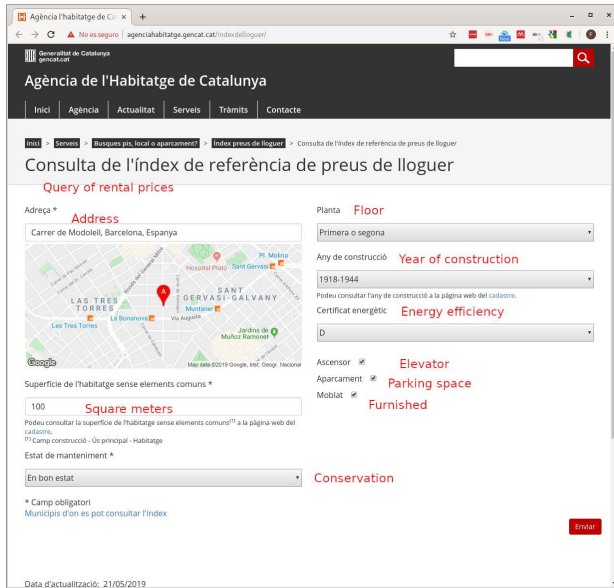
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- Source of information: data on bails deposited *and* rental offers from real state webs; preliminary work is being done with sales data.
- Spatial detail of price indices down to areas a few hundred meters wide..
- A “rent advisor” needs to be programmed, feeding from the same data.



Laspeyres index

- Index at t base 0 defined as

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- We need to observe the prices of all products at 0 and t .

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- No “basket” of houses is repeatedly traded at all times to allow computation of a Laspeyres-type index.
- Plus: opaque market, prices difficult to observe, expensive and slow to survey.

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- Index is then

$$I_{t_0}(t_k) = \exp \left(\sum_{j=0}^k \hat{\gamma}_{t_j} \right) \times 100$$

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- . . .and we need much more information (attributes of each house)

Geographically Weighted Regression (GWR)

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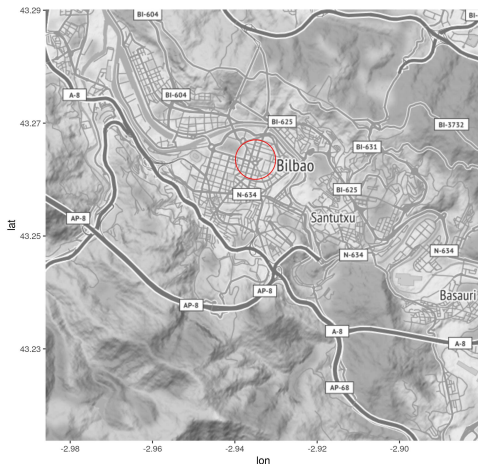
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- With a spline replaced for $\gamma(t)$ this was the model in Barcena et al.(2013).

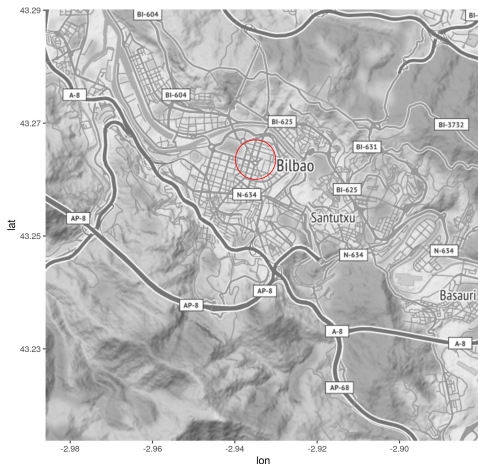
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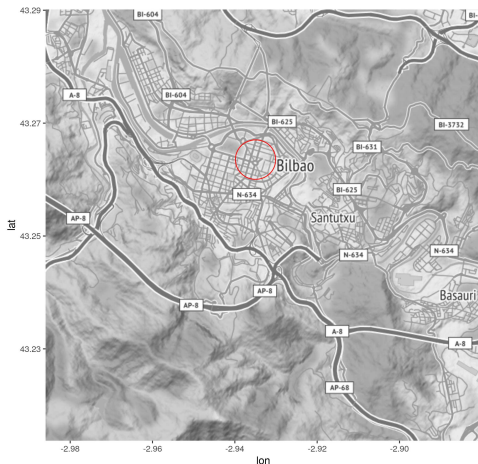
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$$\hat{\gamma}(t) = \arg \min_{i,t} \sum (\hat{\epsilon}_{it} - \gamma(t))^2$$

How do we fit the model? (II)

- Iterate now (1)–(2)–(3) until convergence:

$$\log(P_{it}) - \hat{\gamma}(t) = \sum_k \beta_k(u_i, v_i) x_{ik} + \epsilon \quad (1)$$

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- In all cases we have tried the iteration invariably converges.

What is the result?

- A fitted model **at each location** (u_i, v_i) of the form

$$\log(P_{it}) = \underbrace{\sum_k \hat{\beta}_k(u_i, v_i) x_{ik}}_{\text{Base price}} + \underbrace{\hat{\gamma}(t)}_{\text{Effect of time}} + \hat{\epsilon}$$

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- By-product: shadow prices $\hat{\beta}_k(u_i, v_i)$ at all locations and $t = t_0$

The gory details

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- $\hat{\gamma}(t)$ “smooth”; in our use, a cubic spline (set of cubic polynomials which connect smoothly). Using 1 df per year of data, more than enough.

How to make an index local?

- Ideally, we might fit GWR's for $t = t_0, \dots, t_k$:

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- Price a “median house” at i in times t_0 and t and compute:

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- ...i.e. Laspeyres' index with homogeneous attributes (rather than houses) priced in location i at t_0 and t .
- Heavy computation and data requirements.

Can our model be adapted to do something similar?

$$\log(P_{it}) = \underbrace{\sum_k \hat{\beta}_k(u_i, v_i) x_{ik}}_{\text{Base price}} + \underbrace{\hat{\gamma}(t)}_{\text{Effect of time}} + \hat{\epsilon}$$

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- Want to have $\hat{\gamma}_i(t)$ at each chosen location, rather than a single $\hat{\gamma}(t)$.
- Could repeat the process for each area, but this would neglect information from neighbouring areas.

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- Define $w_{ij} = \left(1 - \frac{d_{ij}}{b}\right)^2$ (or zero if $d_{ij} > b$ for chosen b).

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- In computing $\hat{\gamma}_j(t)$, residuals close in space weighted more.

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- ...but trying to set the two bandwidths by cross-validation very expensive.

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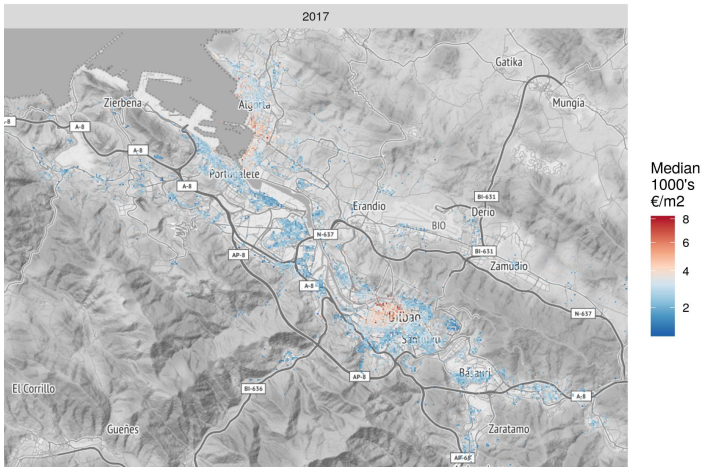
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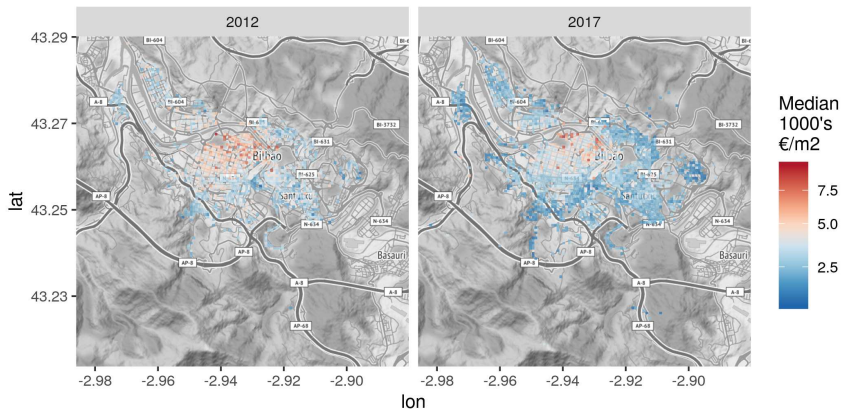
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- Median offered price in thousands of euros color coded.

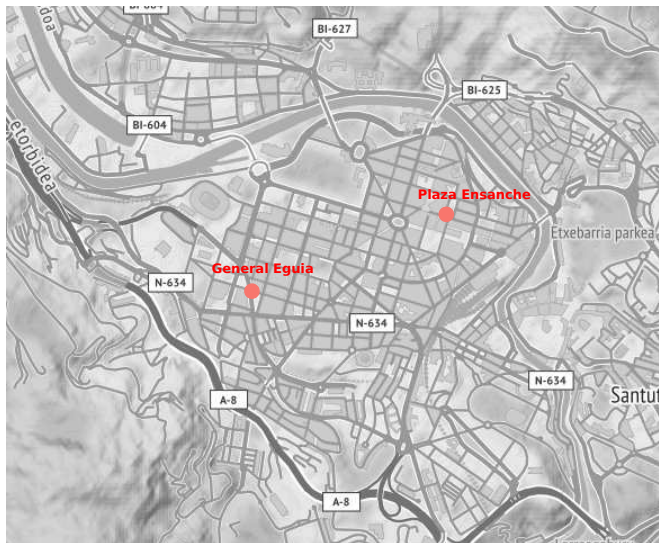
Great Bilbao. Offered prices (1000's €/m²)



Bilbao: 2012 vs 2017



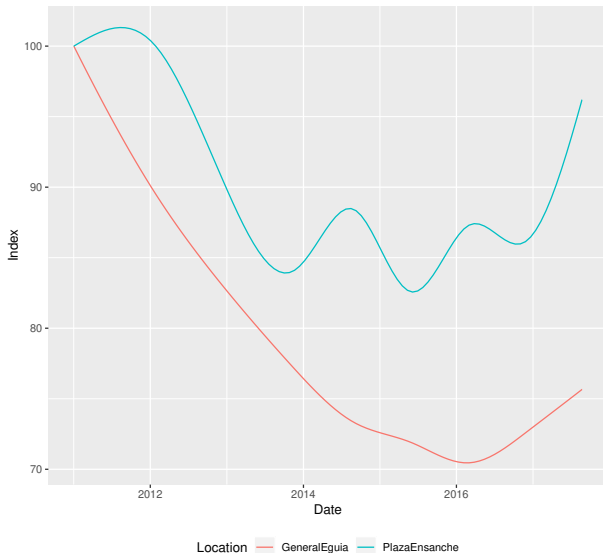
Choice of centroids to investigate different trends



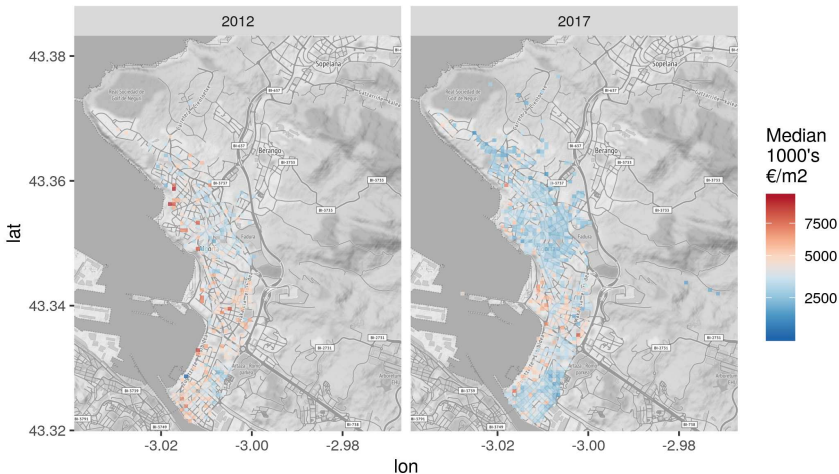
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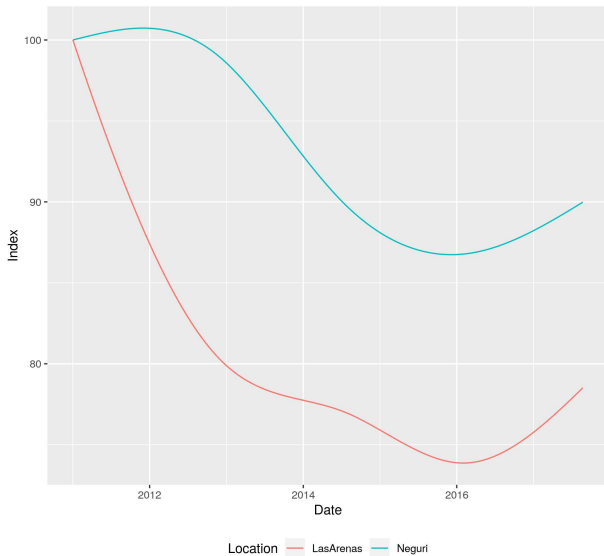
Getxo: 2012 vs 2017



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- In R, several packages provide non-parametric smoothing, including `mgcv` and `gam`.
- Using above packages, it doesn't take much to implement the method described. It has been done in package `ipv`, in GitHub, <https://github.com/FernandoTusell/ipv.git>.

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- Associated paper and slides also available, <https://github.com/FernandoTusell/NBP2019.git>.